



# *New & Recent $B$ -Physics Results on Lifetime and Mixing*

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# Outline

Results presented from BaBar, Belle, DØ, CDF, and Delphi

## ⑥ Lifetime Measurements

- △ Overview
- △ New lifetime ratios
- △ Summary

## ⑥ Mixing Measurements

- △ Overview
- △ New  $B_d$  mixing measurements
- △ New limit on  $B_s$  mixing

## ⑥ $\Delta\Gamma_s/\Gamma_s$ measurement

## ⑥ Summary

# Experimental Overview

## ⑥ *B*-Factories (BaBar, Belle)

- △  $e^+e^- \rightarrow \Upsilon(4S) \rightarrow b\bar{b}$
- △  $\sigma \approx 1 \text{ nb}$
- △ Clean environment

## ⑥ LEP(Delphi)

- △  $e^+e^- \rightarrow Z \rightarrow b\bar{b}$
- △  $\sigma \approx 7 \text{ nb}$
- △ Clean environment
- △ Access to  $B_s, B_c, \Lambda_b, \dots$

## ⑥ Tevatron (DØ, CDF)

- △  $p\bar{p} \rightarrow b\bar{b} + X$
- △  $\sigma \approx 150 \mu\text{b} @ 1.96 \text{ TeV}$
- △ Multiple interactions, hadronic remnants
- △ Access to  $B_s, B_c, \Lambda_b, \dots$



# Lifetime Measurements—Motivation

- ⑥ Lifetimes probe QCD at large distances (*bound state*)
- ⑥ For "Heavy" quarks expect lifetime to be dominated by quark
  - △ Lifetime differences observed in *D*-mesons
  - △ *b* heavier, expect smaller differences ( $\tau(B_{q'})/\tau(B_q) \approx 1$ )
- ⑥ Leading OPE terms in  $\Gamma$  for "heavy" quark hadron decay:
  - △ Spectator term
  - △ Chromomagnetic term ( $1/m_Q^2$  suppression)
  - △ 4-quark interaction term ( $1/m_Q^3$  suppression)
- ⑥ Prediction  $\tau(B_u^+) \geq \tau(B_d^0) \approx \tau(B_s^0) > \tau(\Lambda_b) \gg \tau(B_c^+)$
- ⑥ Experimental numbers given as ratios relative to  $B_d^0$  to reduce systematics



## $\Lambda_b$ Lifetime



### ⑥ New lifetime ratio result from DØ (250 pb<sup>-1</sup>)

$$\Lambda_b \rightarrow J/\psi + \Lambda^0 \rightarrow (\mu^+ \mu^-) + (p\pi^-)$$

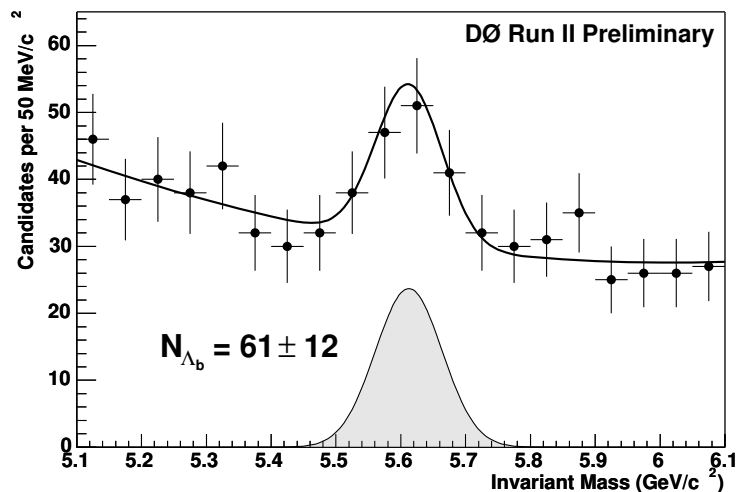
$$B_d^0 \rightarrow J/\psi + K_s^0 \rightarrow (\mu^+ \mu^-) + (\pi^+ \pi^-)$$

- △ Presently theory predicts  $\tau(\Lambda_b)/\tau(B_d^0) \approx 0.9 \pm 0.05$  while the world average is  $0.798 \pm 0.052$
- △ Previous ratio measurements used semileptonic decays
- △ First  $\Lambda_b$  ratio measurement using fully reconstructed decay modes
- △ CDF presented  $\Lambda_b$  lifetime measurement earlier this year using  $\Lambda_b \rightarrow J/\psi + \Lambda^0$

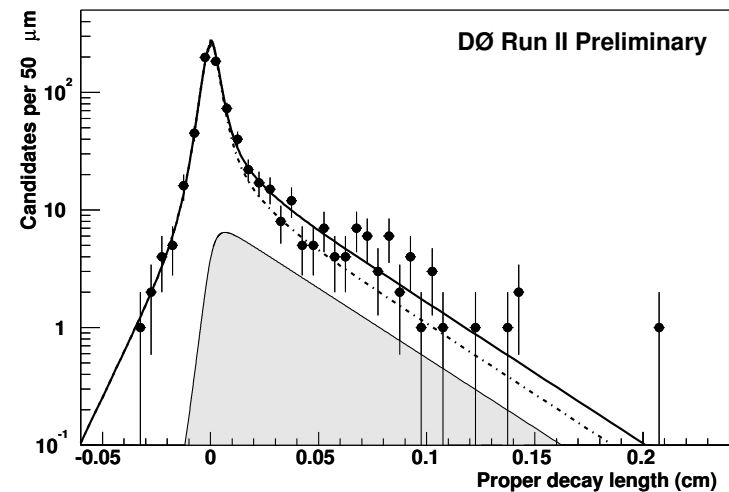


# $\Lambda_b$ Lifetime

## $J/\psi$ - $\Lambda^0$ Mass Distribution



## $J/\psi$ - $\Lambda^0$ Lifetime Distribution



DØ:  $\tau_{\Lambda_b} = 1.221^{+0.217}_{-0.179} \pm 0.043$  ps

CDF:  $\tau_{\Lambda_b} = 1.25 \pm 0.26 \pm 0.10$  ps

World Avg:  $\tau_{\Lambda_b} = 1.229 \pm 0.080$  ps

DØ:  $\tau_{B_d^0} = 1.397^{+0.107}_{-0.098} \pm 0.031$  ps

DØ:  $\tau_{\Lambda_b}/\tau_{B_d^0} = 0.874^{+0.169}_{-0.142} \pm 0.028$

Theory:  $\tau_{\Lambda_b}/\tau_{B_d^0} = 0.9 \pm 0.05$

World Avg:  $\tau_{B_s}/\tau_{B_d^0} = 0.798 \pm 0.052$



## $B_s$ Lifetime



- ⑥ New result from DØ on  $B_s$  to  $B_d$  lifetime ratio

$$B_s^0 \rightarrow J/\psi + \phi \rightarrow (\mu^+ \mu^-) + (K^+ K^-)$$

$$B_d^0 \rightarrow J/\psi + K^{*0} \rightarrow (\mu^+ \mu^-) + (K^+ \pi^-)$$

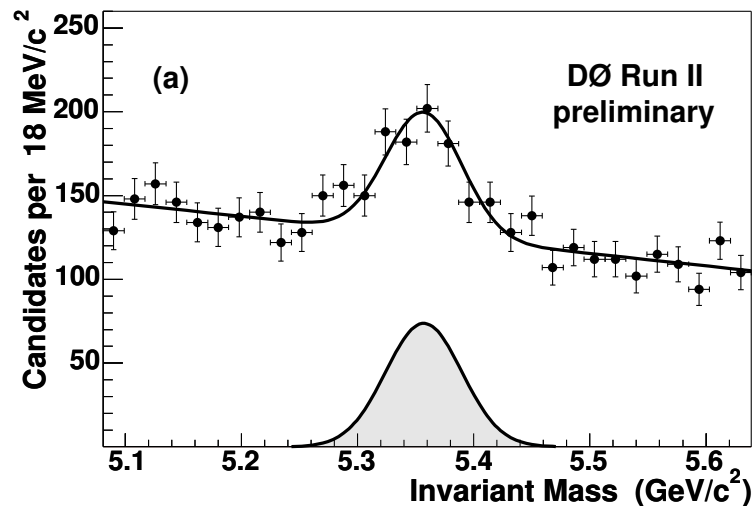
- △ Use fully reconstructed modes to determine ratio
- △ Presently theory predicts  $\tau(B_s)/\tau(B_d^0) = 1.00 \pm 0.01$  while the world average is  $0.951 \pm 0.038$

- ⑥ Recent CDF  $B_s$  lifetime measurement using  $B_s^0 \rightarrow J/\psi \phi$

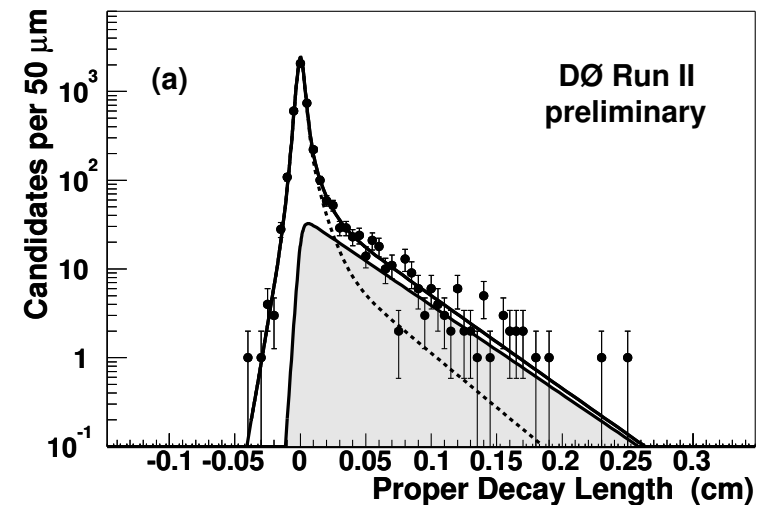


# $B_s$ Lifetime

## $J/\psi$ - $\phi$ Mass Distribution



## $J/\psi$ - $\phi$ Lifetime Distribution



$$D\bar{D}: \tau_{B_s} = 1.444^{+0.098}_{-0.090} \pm 0.020 \text{ ps}$$

$$CDF: \tau_{B_s} = 1.369 \pm 0.100 \pm^{+0.008}_{-0.010} \text{ ps}$$

$$\text{World Avg: } \tau_{B_s} = 1.229 \pm 0.080 \text{ ps}$$

$$D\bar{D}: \tau_{B_d^0} = 1.473^{+0.052}_{-0.050} \pm 0.023 \text{ ps}$$

$$D\bar{D}: \tau_{B_s^0}/\tau_{B_d^0} = 0.980^{+0.075}_{-0.070} \pm 0.003$$

$$\text{Theory: } \tau_{B_s^0}/\tau_{B_d^0} = 1.00 \pm 0.01$$

$$\text{World Avg: } \tau_{B_s}/\tau_{B_d^0} = 0.951 \pm 0.038$$





# $B_u^+$ Lifetime

- ⑥ Recent ratio measurements from DELPHI, DØ, and CDF
  - △ DELPHI uses NN on  $Z \rightarrow b\bar{b}$  ( $1.060 \pm 0.021 \pm 0.024$ )
  - △ DØ uses  $B \rightarrow D^{*-} \mu^+ \nu + X$  dominated by  $B_d^0$  (86%) and  $B \rightarrow \bar{D}^0 \mu^+ \nu + X$  dominated by  $B_u^+$  (82%) ( $250 \text{ pb}^{-1}$ ) ( $1.093 \pm 0.021 \pm 0.022$ )
  - △ CDF uses  $B_d^0 \rightarrow J/\psi + K^{*0}$  and  $B_u^+ \rightarrow J/\psi + K^+$  ( $250 \text{ pb}^{-1}$ ) ( $1.080 \pm 0.042$ )
- ⑥ New ratio measurement from BELLE ( $1.066 \pm 0.008 \pm 0.008$ )
  - △ From  $CP$  asymmetry measurement  $29.1 \rightarrow 140 \text{ fb}^{-1}$
- ⑥ BaBar new  $B_d^0$  lifetime ( $1.501 \pm 0.008 \pm 0.030 \text{ ps}$ )
- ⑥ World Average ( $1.085 \pm 0.017$ )      Theory ( $1.06 \pm 0.02$ )



# Mixing—Overview

- ⑥ Since Mass and Flavor eigenstates not equal, flavor states can mix.
  - △ Requires mass of eigenstates to differ ( $\Delta m_q \neq 0$ )
  - △ Mass eigenstates can have different lifetimes ( $\Delta \Gamma_q \neq 0$ )
  - △ Standard Model expectation  $\Delta m_q \gg \Delta \Gamma_q$

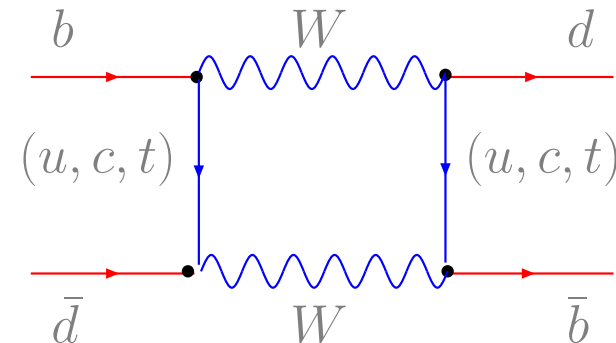
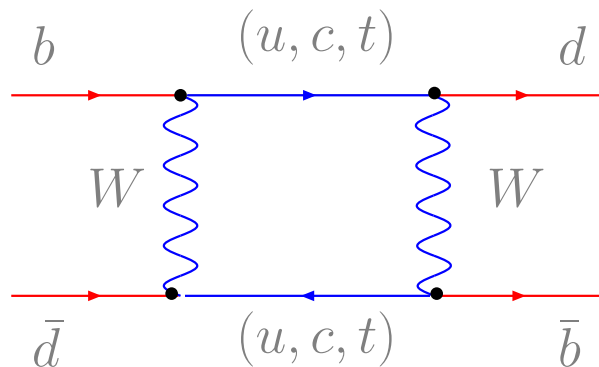
$$\mathcal{P}_{\text{mixed}}^{\text{unmixed}}(t) = \frac{1}{2} \Gamma_q e^{-\frac{\Gamma_q}{2} t} \left[ \cosh \left( \frac{\Delta \Gamma_q}{2} t \right) \pm \cos (\Delta m_q t) \right]$$

Where  $\Gamma_q = \frac{\Gamma_H + \Gamma_L}{2}$  the average of the decay widths of the two mass eigenstates.



# Mixing—Overview

- ⑥ Mixing requires a  $|\Delta B| = 2$  transition ( $B^0 \rightarrow \bar{B}^0$ )



- ⑥ Amplitude is  $\propto |V_{tb}V_{td}|$  because of large  $t$ -quark mass
  - △ Amplitude  $\propto \sum_q S_0 \left( \frac{m_q}{M_W} \right)$



# Mixing—Procedure

## ⑥ Mixing requires measurement of initial and final flavor

### △ Final state tagging examples

$$B_d^0 \rightarrow D^{*-} \mu^+ \nu_\mu$$

$$\bar{B}_d^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$$

$$B_d^0 \rightarrow J/\psi K^{*+} \pi^-$$

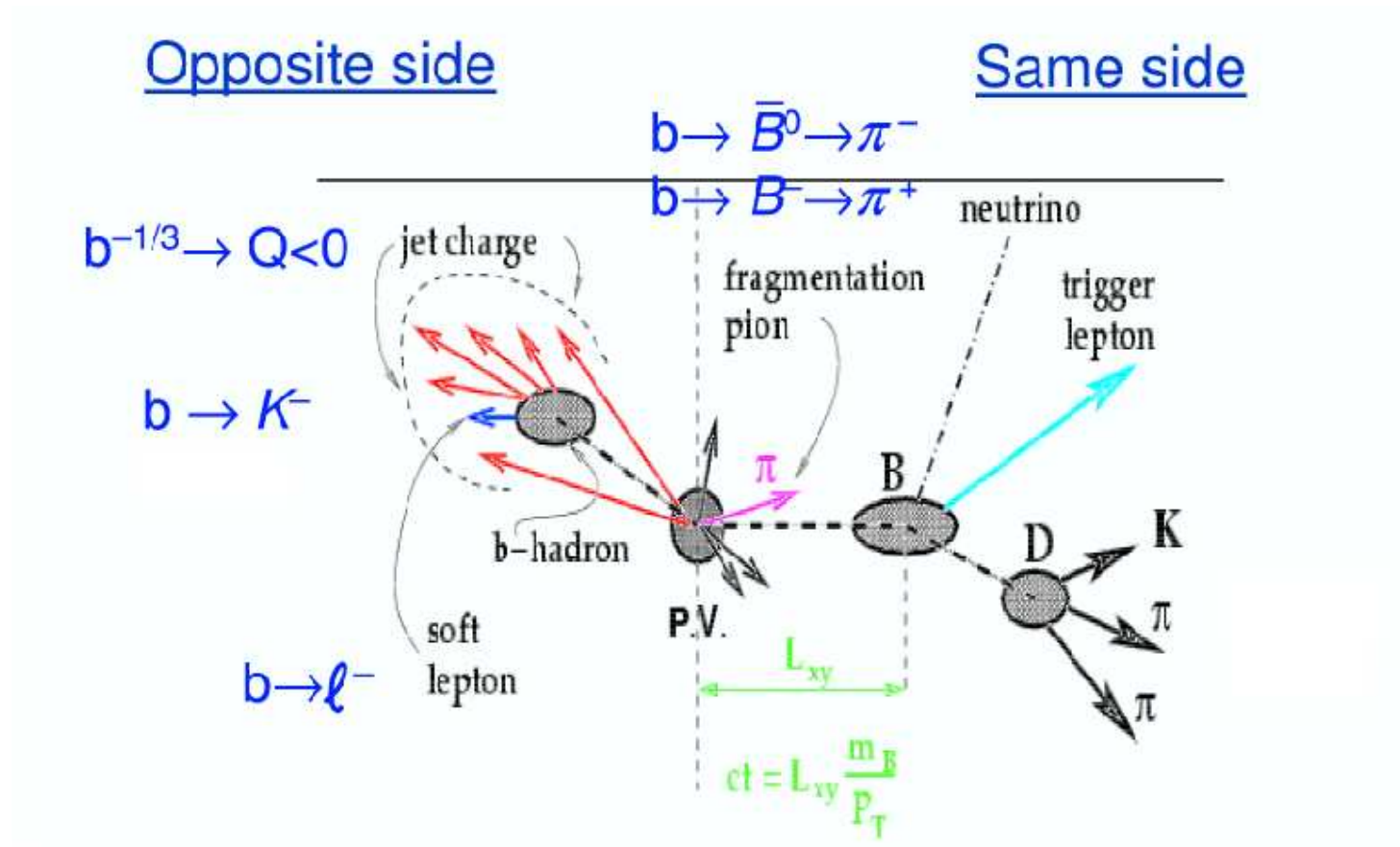
$$\bar{B}_d^0 \rightarrow J/\psi K^{*-} \pi^+$$

- △  $\mu^\pm$  ( $\pi^\pm$ ) provide tag for decay flavor
- △ First set not fully reconstructed,  $\approx 5.4\%$  branching ratio
- △ Second set fully reconstructed,  $\approx 8 \times 10^{-4}$  branching ratio



# Mixing—Procedure

## ⑥ Initial state tagging





- ## CDF

**DØ**

$$B \rightarrow \bar{D}^0 \quad \Rightarrow \quad \begin{cases} B^0 \rightarrow D^{*-} \\ B^+ \rightarrow \bar{D}^0 \end{cases}$$



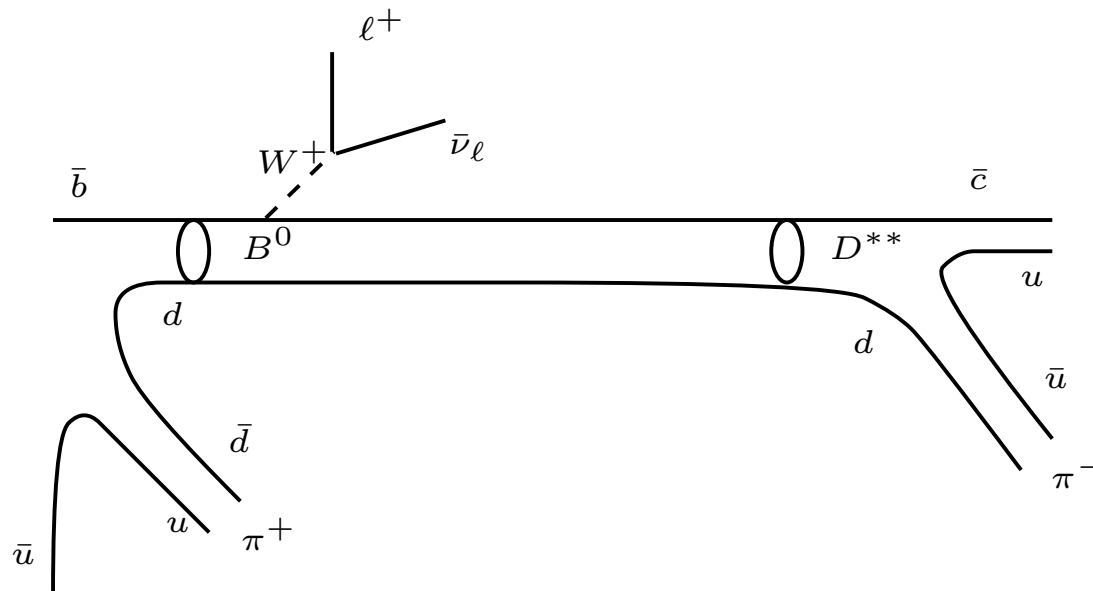


# $B_d$ Mixing—Results

## ⑥ Same Side Tagging Algorithm

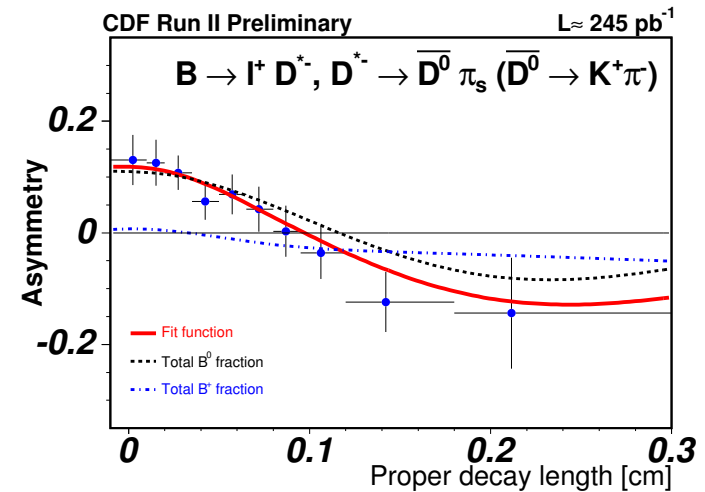
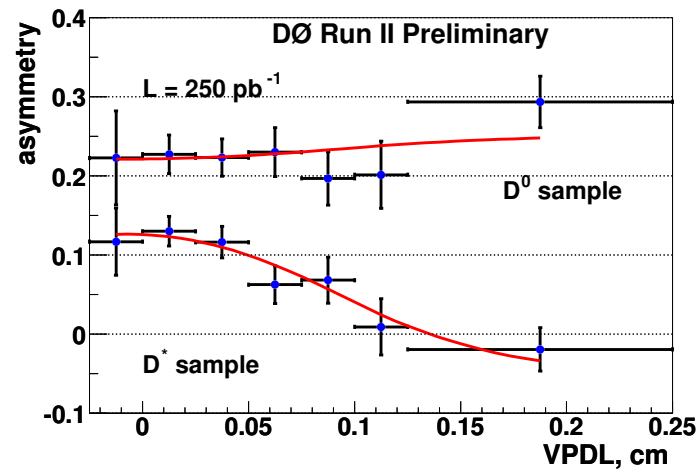
- △ Cone about  $B$ -meson  $\Delta R = 0.7$
- △ Take  $\pi^\pm$  with smallest  $p_T^{\text{rel}}$

## ⑥ Main systematic $\pi^\pm$ from $D^{**}$ decay





# $B_d$ Mixing—Results



## Results

CDF(SST):  $\Delta m_d = 0.443 \pm 0.052 \pm 0.030 \pm 0.012 \text{ ps}^{-1}$

CDF(All):  $\Delta m_d = 0.536 \pm 0.037 \pm 0.009 \pm 0.015 \text{ ps}^{-1}$

DØ(SST):  $\Delta m_d = 0.488 \pm 0.066 \pm 0.044 \text{ ps}^{-1}$

DØ( $O_\mu T$ ):  $\Delta m_d = 0.506 \pm 0.055 \pm 0.049 \text{ ps}^{-1}$

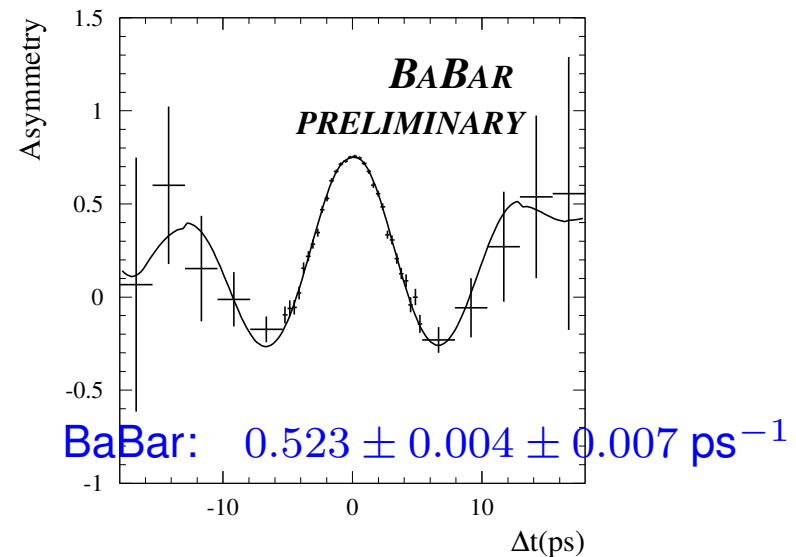
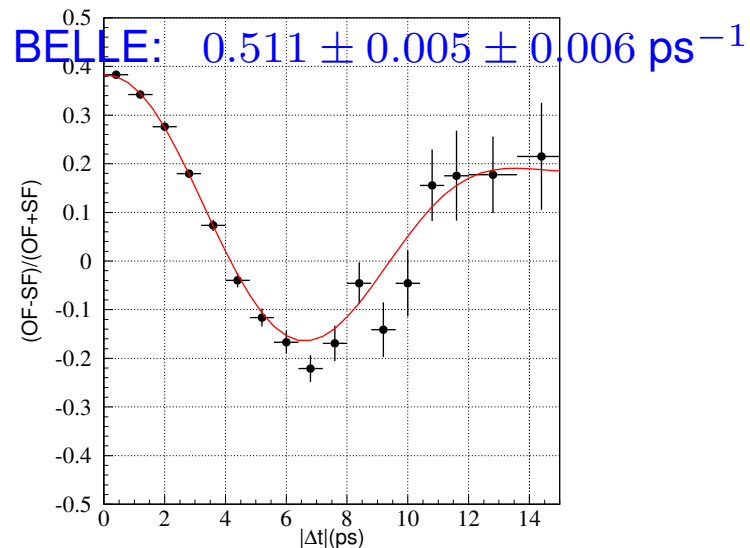
PDG:  $\Delta m_d = 0.502 \pm 0.007 \text{ ps}^{-1}$





# $B_d$ Mixing—Results

- ⑥ New results from BELLE (*by-product of CP asymmetry measurement*) and BaBar
  - △ Use  $B_d^0 \rightarrow D^{*-} \ell^+ \nu$  and fully reconstructed hadronic modes BaBar uses only semi-leptonic mode
  - △ Flavor tag other  $B$  using  $\ell^\pm, \pi^\pm, K^\pm, \Lambda_s^0$  not associated with reconstructed  $B$  BaBar opposite side  $\ell^\pm$  only





## $B_s$ Mixing Limit



- ⑥ DELPHI has produced two new limits on  $B_s$  mixing
- ⑥ Mixing limit obtained using “Amplitude” Method
  - △ Fit data to  $\mathcal{P} = \frac{\Gamma}{2} e^{-\Gamma t} [1 \pm A \cos(\Delta m_s t)]$
  - △ Fit for  $A$  as a function of  $\Delta m_s$ 
    - $A$  peaks at 1 for a measurement
    - Sensitivity given by  $1.645\sigma_A = 1$  95% exclusion
    - Limit given by  $A < 1 - 1.645\sigma_A$  95% exclusion



## $B_s$ *Mixing Limit*



### ⑥ Data samples used for limit

#### △ $\bar{B}_s^0 \rightarrow D_s^+ \ell^- \nu_\ell + X$ Analysis

- $D_s^+ \ell$  is updated result with improved use of proper time resolution
- Sensitivity improved from  $8.4 \text{ ps}^{-1}$  to  $8.6 \text{ ps}^{-1}$

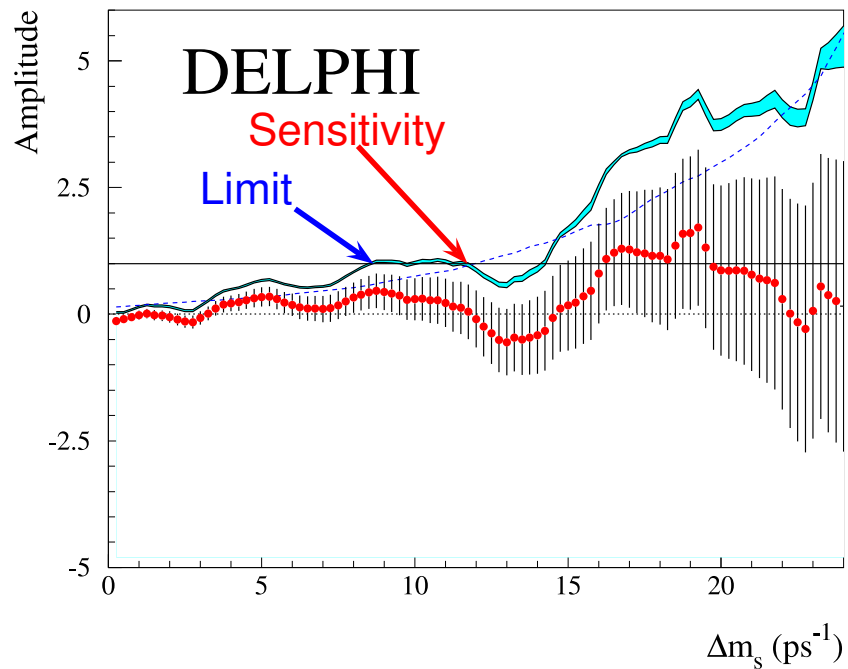
#### △ High $p_T$ Lepton Analysis

- Event divided into 2 hemispheres by plane Transverse to Sphericity axis
- Lepton gives decay tag
- Lifetime from particles in lepton hemisphere
- Production tag from Opposite Side jet charge NN, plus Same Side kaon combined in a single discriminant



# $B_s$ Mixing Limit

## Amplitude Plot



### Limits 95% CL

Lepton Analysis:  $\Delta m_s > 8.0(12.0) \text{ ps}^{-1}$

$D_s + \ell^\pm$  Analysis:  $\Delta m_s > 4.9(8.6) \text{ ps}^{-1}$

All Delphi Analysis:  $\Delta m_s > 8.5(12.0) \text{ ps}^{-1}$

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PDG

$\Delta m_s > 14.4 \text{ ps}^{-1}$

(Sensitivity)



# $\Delta\Gamma_s$ —Overview

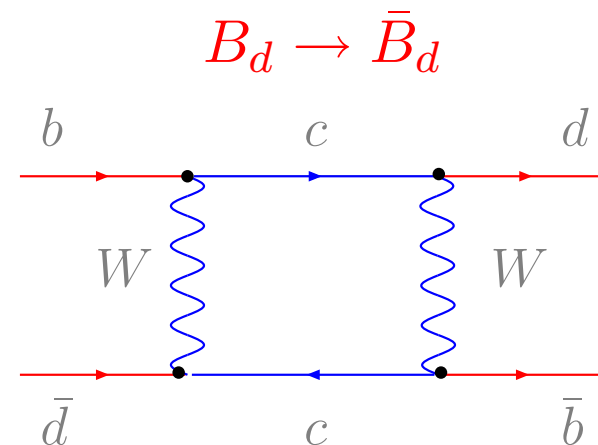
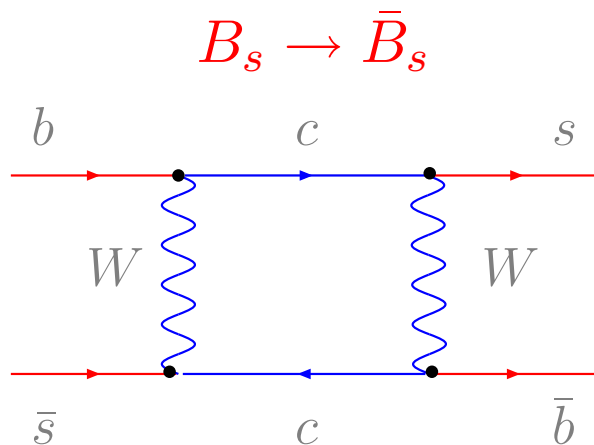
## ⑥ Lifetime of mass eigenstates not expected to be equal

- △  $\Delta\Gamma_q/\Gamma_q$  expected to be small, but since  $\Delta m_s \gg \Delta m_d$  might expect  $\Delta\Gamma_s/\Gamma_s \gg \Delta\Gamma_d/\Gamma_d$

- ..  $\Delta\Gamma_d/\Gamma_d \approx 0.01$        $\Delta\Gamma_s/\Gamma_s = 0.12 \pm 0.06$

Niertse, ... [hep-ph/0012219](#)

- .. Cabbibo allowed  $b \rightarrow c \rightarrow s$  transition for  $B_s$  while Cabbibo suppressed  $b \rightarrow c \rightarrow d$  for  $B_d$





## $\Delta\Gamma_s$ —Analysis

### ⑥ Must separate out two mass eigenstates

- △ These are the  $CP$  even and odd states

$$B_s^H = \frac{1}{\sqrt{2}} [|B_s\rangle + |\bar{B}_s\rangle] \quad CP \text{ odd}$$

$$B_s^L = \frac{1}{\sqrt{2}} [|B_s\rangle - |\bar{B}_s\rangle] \quad CP \text{ even}$$

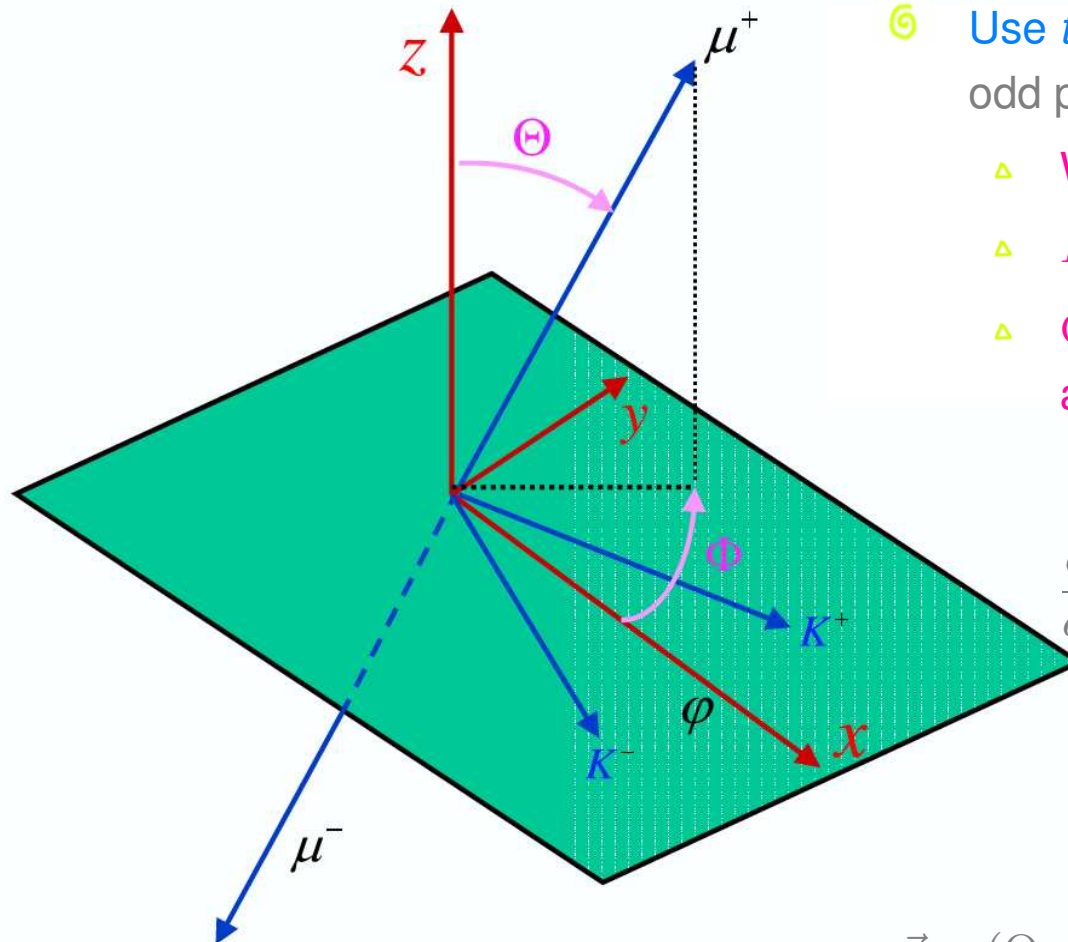
- △ Use  $B_s \rightarrow J/\psi\phi$  w/final state  $J = 0$  since  $J/\psi$  &  $\phi$  have  $S = 1$  this  $\Rightarrow \ell = 0, 1, 2$  ( $S, P, D$  wave)
- △  $S$  &  $D \Rightarrow CP$  even
- △  $P \Rightarrow CP$  odd

### ⑥ Goal is to disentangle different $\ell$ states



# $\Delta\Gamma_s$ Analysis

## Transversity Angles



- ⑥ Use  $B_s \rightarrow J/\psi\phi$  ( $B_d \rightarrow J/\psi K^{0*}$ )
- ⑥ Use *transversity* angles—Separates odd parity states nicely
  - △ Work in  $J/\psi$  rest frame
  - △  $K^+K^-$  defines  $x$ - $y$  plane
  - △  $\Theta, \Phi$  are  $\mu^+$  polar, azimuthal angles,  $\Psi$  helicity angle of  $\phi$

## Angular Distribution $B_s$

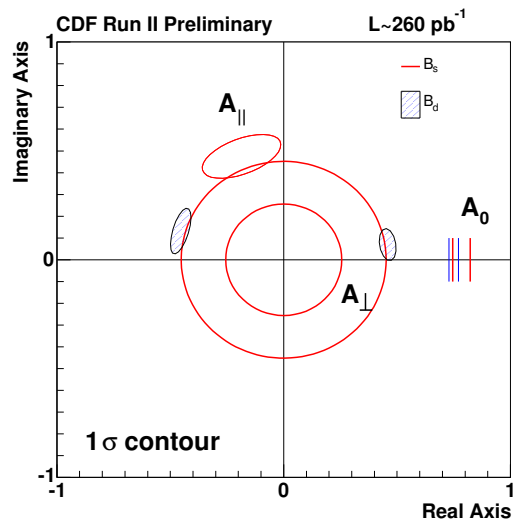
$$\frac{d^4\mathcal{P}}{d\vec{\rho}dt} \propto |A_0|^2 f_1(\vec{\rho}) e^{-\Gamma_L t} + |A_{\parallel}|^2 f_2(\vec{\rho}) e^{-\Gamma_L t} + |A_{\perp}|^2 f_3(\vec{\rho}) e^{-\Gamma_H t} + \text{Re}(A_0^* A_{\perp}) f_5(\vec{\rho}) e^{-\Gamma_L t}$$

$$\vec{\rho} = (\Theta, \Phi, \Psi)$$

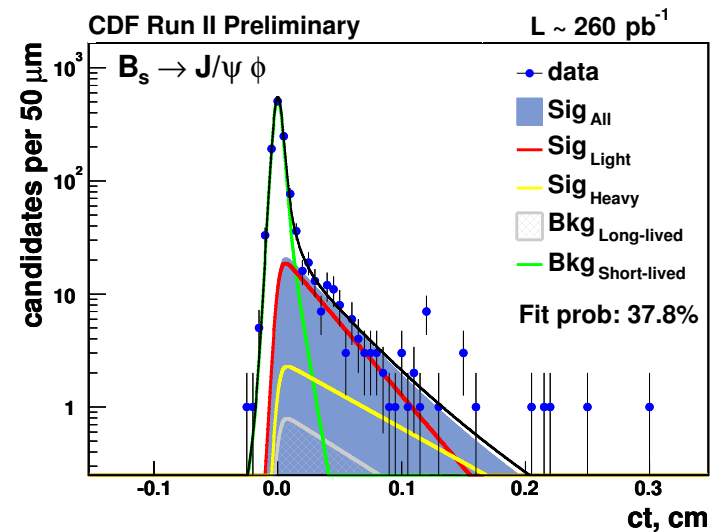


# $\Delta\Gamma_s$ Analysis

## Amplitudes



## Lifetime



## Results

$$A_0 = 0.784 \pm 0.039 \pm 0.007$$

$$A_{\parallel} = (0.510 \pm 0.082 \pm 0.013)e^{(1.94 \pm 0.36 \pm 0.03)i}$$

$$|A_{\perp}| = 0.354 \pm 0.098 \pm 0.003$$

$$\Delta\Gamma_s/\Gamma_s = 0.65_{-0.33}^{+0.25} \pm 0.01$$

$$\Delta\Gamma_s = 0.47_{-0.24}^{+0.19} \pm 0.01 \text{ ps}^{-1}$$

$$\tau_L = 1.05_{-0.13}^{+0.16} \pm 0.02 \text{ ps}$$

$$\tau_H = 2.07_{-0.46}^{+0.58} \pm 0.03 \text{ ps}$$





# Summary

- ⑥ New lifetime ratio measurements for  $B_u^+$ ,  $B_s^0$  and  $\Lambda_b$  vs.  $B_d^0$  from BELLE, CDF, and DØ
  - △ New DØ  $\tau(\Lambda_b)/\tau(B_d^0)$  measurement consistent with theory, higher than world average
- ⑥ New measurements of  $\Delta m_d$ 
  - △ For Tevatron, starting point for measurement of  $\Delta m_s$
- ⑥ New  $\Delta m_s$  limit from DELPHI
- ⑥ CDF measures  $\Delta\Gamma_s/\Gamma_s$